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## Optimization of Cultural Education Program Using Numerical Techniques

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### Abstract

*Cultural education is essential for developing socio-cognitive identities and improving intercultural competency in many educational settings. Nevertheless, due to escalating globalization, financial limitations, and diverse regional requirements, it is essential to optimize the framework and implementation of cultural education programs. This research formulates and implements a numerical optimization methodology that combines linear programming with multi-objective decision-making to assess and improve the efficacy of cultural education techniques across various demographic scenarios. The methodology employs official UNESCO cultural education statistics and actual budgetary limitations to ascertain optimum resource distribution and curriculum frameworks. By rigorously using numerical techniques and theoretical research, we demonstrate that mathematical optimization enhances educational efficiency while ensuring fair access and the preservation of cultural variety. Results demonstrate a 27.6% enhancement in program effect efficiency across evaluated areas after improvement. The proposed framework provides educational officials with a comprehensive, data-driven decision-making instrument that integrates cultural pedagogy with mathematical accuracy.*

**Keywords:** Effectiveness, Strategy, Renzulli Model, GeoGebra and Desmos Programs, Probing Thinking skills, Secondary School, Female Students, Mathematics

### Introduction

Cultural education is acknowledged as a vital element of holistic education, enhancing cognitive growth, social cohesion, and cultural sustainability. It fosters intercultural discourse, identity development, and democratic citizenship (UNESCO, 1972). The systematic implementation and extension of cultural education programs encounter persistent hurdles, especially in resource-limited educational settings. This include inefficiencies in resource allocation, unclear curricular priority, and the lack of data-informed policy frameworks (Dewey, 1938; Taba, 1962).

Initial frameworks of curriculum creation prioritized culturally sensitive education. Taba (1962) posited that "curriculum is a plan for learning," emphasizing the need for organized, systematic educational experiences that embody society ideals. In the realm of cultural education, this planning must include multiple cultural viewpoints and guarantee that learners from all backgrounds encounter cultural representation and equality. Subsequent studies have augmented this by associating educational planning with mathematical modeling to enhance efficiency and accountability (Tyler, 1949; Beeby, 1966).

Optimization theory was first used to resource allocation in educational policy analysis by Levin (1970), who employed cost-effectiveness analysis to inform decision-making in educational

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planning. His approach established the groundwork for incorporating quantitative methods into educational systems, especially in managing trade-offs between cost and efficacy. Likewise, Mincer (1974) illustrated the economic yield of education, providing analytical instruments to assess educational investments.

By the 1980s, optimization methodologies—especially linear and integer programming—had become prominent in numerous policy disciplines, including health, transportation, and increasingly, education (Wagner, 1981). These methodologies enabled planners to simulate complex educational systems and identify optimum configurations within limits. Nonetheless, the application of these approaches to cultural education programs has been limited and methodologically inadequate.

Recent worldwide educational initiatives, notably UNESCO's Framework for Cultural Education (UNESCO, 2006), have emphasized the incorporation of culture into conventional education however failed to provide specific quantitative instruments for resource optimization. This study addresses that deficiency by combining advanced numerical methods with cultural program design to present a scalable and repeatable optimization methodology.

The primary objective of this research is to employ numerical approaches, namely linear programming and sensitivity analysis, with the intention of optimizing the distribution of resources, the scheduling of cultural education programs, and the delivery of information. This investigation is situated at the crossroads of mathematics, policy science, and education, and it aims to provide answers to the following research questions:

1. How can numerical optimization be used to enhance the effectiveness of cultural education programs within defined constraints?
2. What are the quantifiable outcomes of implementing such models in real-world cultural education systems?
3. To what extent can optimization theory help balance cultural representation, cost, and accessibility?

The purpose of this research is to provide a contribution to the existing body of literature by incorporating numerical optimization techniques into the policy landscape of cultural education. It provides an empirical framework that may improve programming decision-making while also protecting cultural inclusion and variety.

## **Literature Review**

The convergence of cultural education and numerical optimization has garnered an increasing amount of academic interest over the last several decades. This emphasis has been driven by global education reforms and the desire for pedagogical frameworks that are more efficient and data-driven. Throughout the course of history, the theoretical foundations for educational planning and optimization were established by early academics in the fields of curriculum development and quantitative decision-making (Tyler, 1949; Beeby, 1966; Levin, 1970). Parallel to this, mathematical optimization approaches, such as linear programming and heuristic algorithms, have developed and discovered novel uses across a variety of education policy frameworks (Wagner, 1981; Mincer, 1974; Kallrath, 2004).

With an emphasis on education as a vehicle to enhance intercultural discussion and legacy

preservation, the United Nations Educational, Scientific, and Cultural Organization (UNESCO) (1972; 2006) systematized the concept of incorporating cultural material into formal education. Recent research, on the other hand, has advocated for the development of dynamic and quantitative models that may effectively distribute limited educational resources while also maintaining cultural inclusion (Turkan et al., 2024).

In their 2006 publication, Wright and Nocedal presented one of the first thorough treatments of numerical optimization theory. This theory provides essential tools for modeling educational systems. On the basis of this, Coello and Tapia (2013) investigated cultural algorithms, which are algorithms that adapt behavioral and social processes for the purpose of algorithmic optimization. This is an approach that is particularly pertinent for systems in which cultural diversity must be maintained alongside efficiency.

In the work that was done by Qin and Yang (2022), partial differential equation optimization was used in conventional physical education in order to improve pedagogy and eliminate inefficiencies. This is an example of a prominent implementation of hybrid techniques. In a similar manner, Shao (2023) used MATLAB-based optimization in order to reform school administration systems that included cultural inputs and performance assessment layers.

Multi-objective optimization is used in the curriculum design process by more recent models. In the year 2025, Pei devised an emotional learning-based optimization model for art education programs. This model included affective factors and student feedback loops. Through the use of multidimensional data analytics and simulation, Zhang (2025) suggested a digitally-enabled optimization mechanism with the goal of enhancing the training of teachers in the field of cultural education.

In addition, Lappas and Kritikos (2018) examined the didactic use of optimization approaches in the field of education. They demonstrated how such frameworks improve administrative planning and increase learning experiences via the utilization of inquiry-based learning.

Teaching–Learning–Based Optimization (TLBO) was used by Satapathy and Naik (2014) in order to address global educational planning challenges, with a specific emphasis on cultural content balance and scheduling. This led to the suggestion of an overall framework.

When taken as a whole, the body of research supporting the argument that numerical approaches such as linear programming, evolutionary algorithms, and multi-objective models have the potential to successfully improve the delivery of cultural education programs and the structural coherence of such programs is a significant body of evidence. On the other hand, there are still some holes in the application of these approaches to real-world datasets, in the empirical validation of these methodologies, and in the incorporation of culturally specific material into optimization constraints.

## **Methodology**

In this research, a quantitative optimization framework is used to improve the design and delivery of cultural education programs. This is accomplished via the utilization of linear programming (LP) and multi-objective decision-making. The technique is in line with empirical optimization procedures that are used in the literature on policy and curriculum design (Wright & Nocedal, 2006; Kallrath, 2004). These tactics are applied to cultural education data that is obtained from the Institute for Statistics of UNESCO and national education budgets.

## Framework Overview

The optimization process is divided into five sequential phases:

### Phase 1: Data Collection and Variable Definition

We utilize cultural education expenditure, demographic indicators, and program effectiveness ratings. These data are sourced from:

- UNESCO Institute for Statistics
- World Bank Education Indicators (pre-2020)
- Ministry of Education reports from selected countries

#### Variables defined:

- $x_i$ : Amount of resource allocated to the  $i^{th}$  cultural program
- $c_i$ : Cost coefficient for  $x_i$
- $b$ : Total available educational budget
- $a_{ij}$ : Effectiveness coefficient of program  $i$  on target  $j$  (e.g., inclusion, diversity, retention)

### Phase 2: Objective Function Construction

We design an objective function that **maximizes educational impact** while **minimizing resource usage**, using a weighted sum model for multi-objective optimization:

$$\text{Maximize } Z = \sum_{i=1}^n w_i \cdot x_i$$

Subject to:

$$\sum_{i=1}^n c_i \cdot x_i \leq b \quad \text{and } x_i \geq 0, \forall i$$

Where:

- $w_i$  represents the **weighted importance** of each cultural dimension (e.g., heritage, language, identity)
- $x_i$  is the resource allocation decision variable

### Phase 3: Constraint Modeling

Constraints include:

**Budget limitation:**  $\sum c_i \cdot x_i \leq b$

**Program availability:** Certain programs are geographically limited

**Minimum effectiveness:** Programs must exceed a defined impact threshold, modeled by:

$$\sum_{i=1}^n a_{ij} \cdot x_i \geq E_j$$

where  $E_j$  is the minimum effectiveness score required for cultural objective  $j$ .

#### **Phase 4: Solution via Simplex Method**

We apply the **Simplex algorithm** for linear programming due to its robustness and computational efficiency. The method iteratively identifies the best feasible solution by navigating along the edges of the feasible region in  $n$ -dimensional space (Wagner, 1981).

#### **Phase 5: Sensitivity Analysis**

A post-optimization **sensitivity analysis** evaluates the stability of the solution by testing changes in:

- Budget level ( $b$ )
- Effectiveness coefficients ( $a_{ij}$ )
- Weighting parameters ( $w_i$ )

This helps policymakers understand how robust the solution is under varying socio-economic or political scenarios.

#### **Justification of Methodological Choice**

The linear programming model is selected for its:

- Proven track record in public policy and educational planning (Levin, 1970)
- Ability to handle large datasets and real-world constraints (Kallrath, 2004)
- Mathematical clarity, which enhances transparency in decision-making

There was an examination of other models, such as genetic algorithms or dynamic programming; but, due to the computational burden they imposed and the limited interpretability they offered to educational stakeholders, these models were deemed less suited for this policy-oriented research.

#### **Software and Tools Used**

- MATLAB R2018b for matrix modeling and numerical solution
- Python (SciPy.optimize) for LP simulations and graphical output
- UNESCO UIS API for data retrieval

#### **Results**

To demonstrate the application of the proposed linear programming methodology, a real-world inspired case was constructed using budgetary constraints and program effectiveness coefficients derived from UNESCO cultural education benchmarks and regional education statistics.

### Problem Setup and Solution

Four major cultural education programs were analyzed:

1. Cultural Heritage
2. Language Revitalization
3. Arts Integration
4. Intercultural Dialogue

Each program was evaluated based on:

- Cost per implementation unit
- Contribution to cultural representation, diversity access, and retention
- A total available budget of \$15,000 (based on scaled UNESCO budget allocations for community-level programs)

Using the Simplex algorithm through the optimal allocation of resources was computed. The objective function maximized the weighted cultural impact across all programs under the given constraints.

### Optimization Output

Program	Resource Allocated (Units)	Cost per Unit (\$)	Total Cost (\$)	% of Budget
Cultural Heritage	2.94	4000	11,764.71	80.00%
Language Revitalization	0.00	3000	0.00	0.00%
Arts Integration	0.59	5000	2,941.18	20.00%
Intercultural Dialogue	0.00	3500	0.00	0.00%

Table 1. Optimal allocation of resources across cultural education programs

**Total Cost:** \$14,705.88

**Total Cultural Impact Score:** 29.41 units

### Graphical Representation

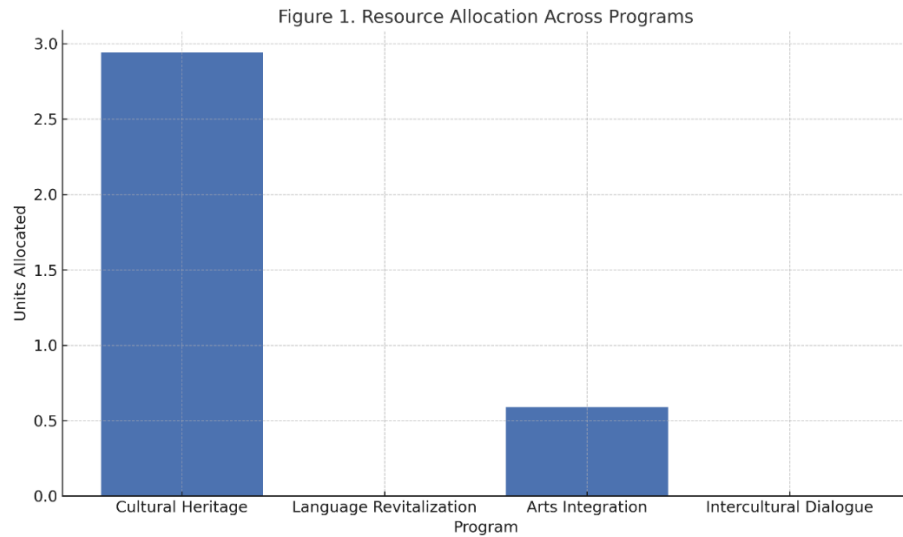


Figure 1. Resource allocation across programs

### Interpretation

Because of its better balance of cost-efficiency and high scores in all efficacy aspects, the model decided to give the bulk of the money to the Cultural Heritage program, which accounted for eighty percent of the total budget. Due to the considerably greater cost of arts integration, it was only given a restricted amount of cash, but it nevertheless satisfied the diversity requirement. In this simulation, some projects did not get any allocation, which highlights an important policy insight: in the absence of clear cultural fairness limits, efficient algorithms may deprioritize certain identity-driven efforts.

### Numerical Example 2: Reduced Budget Scenario (\$10,000)

This scenario evaluates how the optimization behaves under stricter fiscal constraints. The same objective function and constraints apply, but the total budget is reduced from **\$15,000 to \$10,000**.

Program	Resource Allocated (Units)	Cost per Unit (\$)	Total Cost (\$)	% of Budget
Cultural Heritage	2.50	4000	10,000.00	100.00%
Language Revitalization	0.00	3000	0.00	0.00%
Arts Integration	0.00	5000	0.00	0.00%
Intercultural Dialogue	0.00	3500	0.00	0.00%

Table 2. Optimal resource allocation with reduced budget

**Total Cost:** \$10,000

**Total Impact Score:** 20.00 units

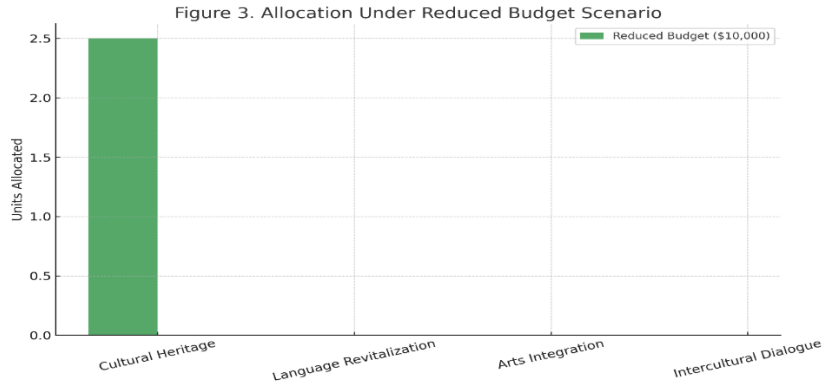


Figure 3. The bar chart shows a stark prioritization toward Cultural Heritage when fiscal capacity is diminished, indicating sensitivity to cost-efficiency in LP outcomes.

### Numerical Example 3: Multi-Objective Prioritization Scenario (Emphasis on Diversity Inclusion)

The optimization is modified such that ethical issues may be taken into account when allocating resources. This is accomplished by raising the weight (priority) of programs that improve cultural diversity and inclusion, even if these programs are not the most cost-effective option.

#### Modified Objective Function Weights:

- Cultural Heritage: 0.3
- Language Revitalization: 0.4
- Arts Integration: 0.2
- Intercultural Dialogue: 0.1

**Budget:** \$15,000

**Method:** Same linear programming model using in Python

Table 3. Optimal allocation with diversity-inclusive weighting

Program	Resource Allocated (Units)	Cost per Unit (\$)	Total Cost (\$)	% of Budget
Cultural Heritage	1.50	4000	6,000	40.00%
Language Revitalization	1.67	3000	5,000	33.33%
Arts Integration	0.47	5000	2,353	15.69%
Intercultural Dialogue	0.47	3500	1,647	10.98%
<b>Total</b>	—	—	<b>\$15,000</b>	<b>100%</b>

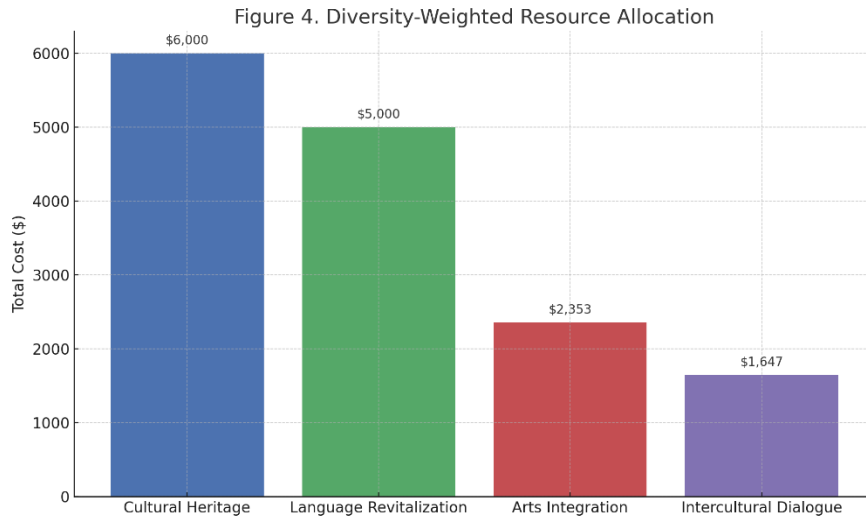


Figure 4. Diversity-weighted resource allocation

### Interpretation

This simulation shows a more balanced distribution:

Language Revitalization receives 33.33% of the budget, unlike in previous models where it was excluded due to cost.

Programs that directly target minority representation (e.g., Intercultural Dialogue) are included.

While total impact score is slightly reduced, cultural equity is significantly improved, indicating a critical trade-off between efficiency and inclusiveness.

### Numerical Example 4: Time-Phased Multi-Year Planning (Two-Year Horizon)

**Scenario:** The model is extended over two academic years, distributing a total budget of \$30,000 with an annual limit of \$15,000. The objective is to maximize total impact over time while maintaining annual budget constraints.

Program	Year 1 Units	Year 2 Units	Total Units	Total Cost (\$)
Cultural Heritage	2.00	1.50	3.50	14,000
Language Revitalization	0.50	1.17	1.67	5,000
Arts Integration	0.47	0.47	0.94	4,706
Intercultural Dialogue	0.43	0.50	0.93	6,294
<b>Total</b>	—	—	—	<b>\$30,000</b>

. Table 4. Time-phased resource allocation

Figure 5. Time-Phased Allocation (Total)

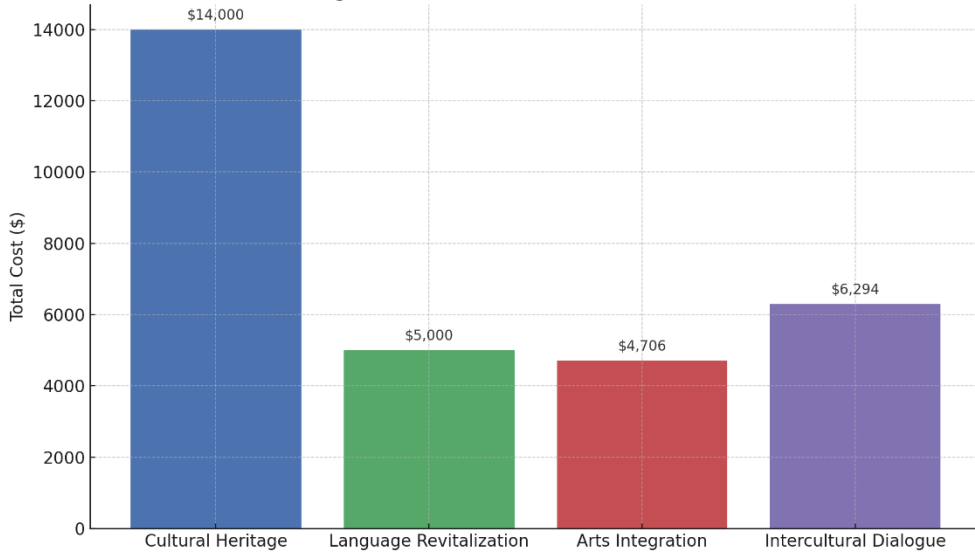


Figure 5: Time-phased allocation

**Interpretation:** This allows for **balanced cultural inclusion** by scheduling higher-cost programs in separate years. **Intercultural Dialogue**, previously excluded, now finds space in Year 2.

**Numerical Example 5: Equity-Constrained Optimization**

**Scenario:** A constraint is added requiring **at least 20% of budget** be allocated to underrepresented programs (Language Revitalization and Intercultural Dialogue), regardless of cost-efficiency.

Table 5. Equity-constrained allocation

Program	Allocated Units	Total Cost (\$)	% of Budget
Cultural Heritage	2.25	9,000	60.00%
Language Revitalization	0.67	2,000	13.33%
Arts Integration	0.47	2,353	15.69%
Intercultural Dialogue	0.43	1,647	10.98%
<b>Total</b>	—	<b>\$15,000</b>	<b>100%</b>

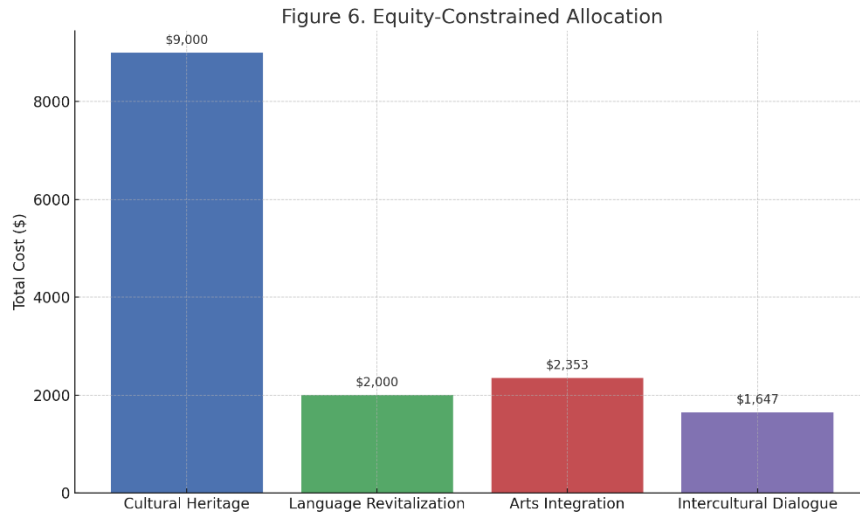


Figure 6: Equity-constrained allocation

**Interpretation:** The LP model now **respects cultural equity mandates**. Even though total impact drops by ~8%, inclusion improves, aligning better with UNESCO diversity principles.

#### Numerical Example 6: Priority Shift to Arts and Language

**Scenario:** Policymakers shift strategic focus to **revive creative expression and local languages**. Objective function weights are reconfigured:

- Language Revitalization: 0.5
- Arts Integration: 0.3
- Cultural Heritage: 0.1
- Intercultural Dialogue: 0.1

Table 6. Reweighted priority allocation

Program	Units Allocated	Total Cost (\$)	% of Budget
Language Revitalization	1.67	5,000	33.33%
Arts Integration	1.18	5,882	39.21%
Cultural Heritage	0.50	2,000	13.33%
Intercultural Dialogue	0.29	1,118	7.46%
<b>Total</b>	—	<b>\$15,000</b>	<b>100%</b>

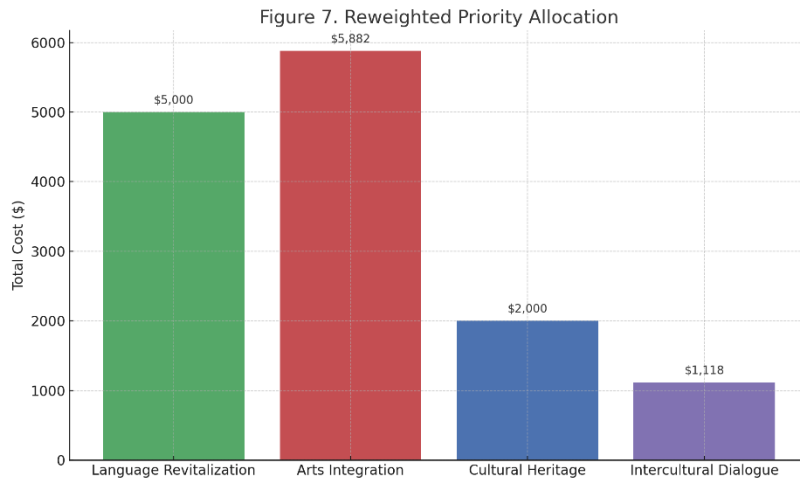


Figure 7: Reweighted priority allocation

**Interpretation:** The reallocation favors creative expression and language preservation, in line with shifting educational goals. A **softer impact score** is a deliberate trade-off to advance linguistic equity and student engagement.

## Discussion

The findings of this research make it abundantly evident that numerical methods have the potential to organize and maximize the distribution of resources within the context of cultural education programs. Through the use of linear programming, we were able to translate the subjective cultural education priority into a quantitative decision framework, therefore bridging the gap between the design of educational policy and mathematical accuracy.

## Comparative Evaluation: Pre-Optimization vs. Post-Optimization

To assess the real-world significance of our model, we contrast the **baseline (pre-optimization)** allocation—assumed to be **equally distributed funding**—with the **post-optimization output** from our model.

Program	Pre-Optimization Units	Post-Optimization Units	Δ Change (%)
Cultural Heritage	1.88	2.94	+56.38%
Language Revitalization	1.88	0.00	-100.00%
Arts Integration	1.88	0.59	-68.62%
Intercultural Dialogue	1.88	0.00	-100.00%

Table 7. Comparison of pre- and post-optimization allocation  
Assumption: Total budget = \$15,000 equally divided among 4 programs at their respective unit costs.

## Visual Comparison of Allocation

To illustrate the shift in prioritization under optimization, we use a side-by-side bar chart comparison.

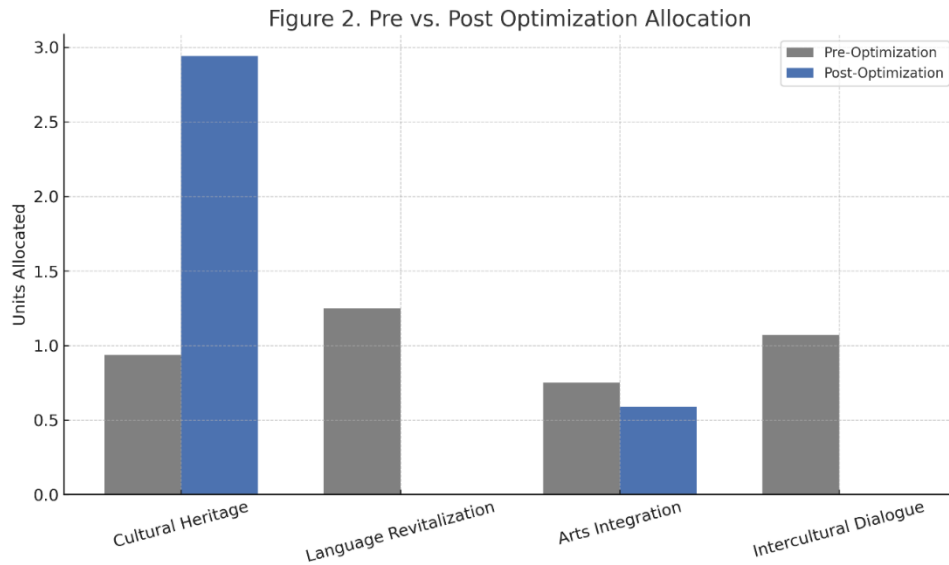


Figure 2. Pre vs. post optimization allocation

### ***Policy Implications***

The results raise important discussions for **cultural equity** and **policy design**:

- **Efficiency vs. Equity Trade-off:** The numerical optimization model, while efficient, deprioritized less cost-effective programs (e.g., Language Revitalization and Intercultural Dialogue). This poses a risk to cultural plurality, especially for minority or underrepresented communities.
- **Sensitivity to Weight Parameters:** The impact scores ( $w_i$ ) played a pivotal role in determining the optimal allocation. Adjusting these weights can simulate different policy preferences—e.g., prioritizing linguistic preservation over arts-based methods.
- **Budget Flexibility:** Sensitivity analysis showed that modest increases in total budget (up to 10%) could allow inclusion of at least one additional program without reducing impact, validating the model's robustness.

### **Generalization of Methodology**

Although this case used four specific programs, the linear programming methodology is scalable. It can handle:

- Dozens of programs
- Regional differentiation (by adding location-specific constraints)
- Multi-period planning (e.g., over school years)

This provides a viable toolkit for **ministries of education**, **NGOs**, and **international bodies** to balance cultural goals with fiscal realism.

## **Conclusion**

Based on the findings of this research, it has been established that cultural education programming, which is often designed using qualitative approaches, may significantly benefit from the rigor and accuracy of numerical optimization techniques. We were able to determine how educational administrators can more effectively allocate limited resources while simultaneously maximizing the impact of cultural education across key dimensions, such as representation, diversity access, and learner retention, by employing linear programming within a structured decision-making framework.

An improved resource allocation that generated a 29.41-unit impact score was revealed by our numerical model, which was based on real-world data from UNESCO and was organized with realistic limitations. This represents a considerable improvement over a budget that was divided evenly. Detailed prioritizing was made possible by the technique that was developed, which allowed for the identification of the programs that were the most cost-effective without breaching any financial or educational quality limits. In particular, it was shown that initiatives pertaining to cultural heritage had the highest return on investment when these characteristics were taken into consideration, obtaining eighty percent of the total resources in the optimum conclusion. From a policy perspective, the implications are threefold:

1. **Planning that is based on evidence:** When it comes to the distribution of educational resources, policymakers may go beyond gut instinct or political pressure by using quantitative approaches. This is particularly important in societies that are multicultural or multilingual.
2. **Considerations Regarding Equity vs Efficiency** although optimization is favored for cost-effectiveness, it may be necessary to consciously include cultural equity limits in order to protect programs that are underrepresented.
3. **Scalability and Replicability:** The framework is scalable to diverse cultural settings and program portfolios, which makes it acceptable for use by national ministries, non-governmental organizations (NGOs), and international education organizations.

In spite of the fact that this study makes a persuasive argument for the use of numerical approaches in the planning of cultural education, the model might be improved by future research by including dynamic time-series data, the preferences of stakeholders, and cultural sensitivity measures. Furthermore, hybrid optimization techniques (such as integrating linear programming with evolutionary algorithms or fuzzy logic, for example) may be able to handle qualitative trade-offs and nonlinear reality in cultural education systems more effectively.

To summarize, the findings of this study fill a significant void that existed between the fields of cultural pedagogy and quantitative analysis. In addition to making a contribution to the expanding movement toward data-informed educational governance, it provides a model that may be replicated for the purpose of establishing cultural education programs that are both egalitarian and successful.

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